

$$\prod_{v \in \Omega} X(k_v) = \left\{ (P_v) \in \prod_{v \in \Omega} X(k_v) : (\exists S \subset \Omega \text{ finite}) (\forall v \notin S) P_v \in X(\mathcal{O}_v) \right\}$$